Chemistry 12
Equilibrium III

## Name:

Date:
Block:

1. The Haber-Bosch Process
2. $K_{\text {eq }}$

## The Haber-Bosch Process



It has been called one of the greatest inventions of the $20^{\text {th }}$ Century, and without it almost half the world's population would not be alive today.

Two German chemists, Fritz Haber and Carl Bosch, devised a way to transform nitrogen in the air (78\%) into fertilizer, using what became known as the Haber-Bosch process.

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})} \quad \Delta \mathrm{H}=-92 \mathrm{~kJ} / \mathrm{mol}
$$

In order to form the desired product, you need to generate extreme heat and pressure. To create these conditions the Haber-Bosch process today consumes more than $1 \%$ of all the world's energy. (Think about the carbon emissions). Only some of the nitrogen in fertilizer makes its way via crops to humans.

German chemist Fritz Haber developed the equipment and procedures from producing ammonia $\left(\mathrm{NH}_{3}\right)$ from its constituent elements ( $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ ) in 1910. In 1918, he received the Nobel Prize in chemistry for his accomplishment. In 1931, another German chemist, Carl Bosch, won the Nobel Prize in chemistry, in part for transforming the process to an industrial scale.

## The Equilibrium Constant

Consider the following equation:

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})}
$$

At equilibrium, the forward and reverse rates are equal.

> Forward rate:

Reverse rate:

Rearranging to isolate the constants, we get:

In this case, $\frac{\mathrm{k}_{\mathrm{f}}}{\mathrm{k}_{\mathrm{r}}}$ provides a constant that chemists call the equilibrium constant, $\mathbf{K}_{\text {eq }}$.

$$
\mathrm{K}_{\mathrm{eq}}=
$$

Regardless of the initial concentrations of reactants and products, when equilibrium is achieved and the equilibrium concentrations are substituted into this expression, the calculated value will always be the same.

The equilibrium law states that for the general balanced equation:

$$
\mathbf{w A}+\mathbf{x B} \leftrightharpoons \mathbf{y C}+\mathbf{z D}
$$

where $\mathrm{w}, \mathrm{x}, \mathrm{y}$ and z are coefficients to balance the equation.

Balance and write the equilibrium expression for the following reactions:
$\ldots \mathrm{C}_{2} \mathrm{H}_{2(\mathrm{~g})}+\ldots \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons \ldots \mathrm{CH}_{4(\mathrm{~g})}$
$\ldots \mathrm{SO}_{2(\mathrm{~g})}+\ldots \mathrm{O}_{2(\mathrm{~g})} \leftrightharpoons \ldots \mathrm{SO}_{3(\mathrm{~g})}$
$\ldots \mathrm{HCl}_{(\mathrm{g})}+\ldots \mathrm{O}_{2(\mathrm{~g})} \leftrightharpoons \ldots \mathrm{Cl}_{2(\mathrm{~g})}+\ldots \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})} \quad$ _ $\mathrm{CH}_{4(\mathrm{~g})}+\ldots \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})} \leftrightharpoons$ _ $\mathrm{CO}_{(\mathrm{g})}+\ldots \mathrm{H}_{2(\mathrm{~g})}$

1. The following gases are at equilibrium in a flask at $423^{\circ} \mathrm{C}$ :
$4.56 \times 10^{-3} \mathrm{M} \mathrm{H}_{2}, 7.4 \times 10^{-4} \mathrm{M} \mathrm{I}_{2}$, and $1.35 \times 10^{-2} \mathrm{M} \mathrm{HI}$. What is the equilibrium constant for the reaction at this temperature?

$$
\ldots \mathrm{H}_{2(\mathrm{~g})}+\ldots \mathrm{I}_{2(\mathrm{~g})} \leftrightharpoons \ldots \mathrm{HI}_{(\mathrm{g})}
$$

2. A quantity of $3.88 \times 10^{-3} \mathrm{M} \mathrm{NO}_{2}$ is at equilibrium with $1.73 \times 10^{-4} \mathrm{M} \mathrm{N}_{2} \mathrm{O}_{4}$ at $60^{\circ} \mathrm{C}$. What is the equilibrium constant for the reaction?

$$
\ldots \mathrm{NO}_{2(\mathrm{~g})} \leftrightharpoons \ldots \mathrm{N}_{2} \mathrm{O}_{4(\mathrm{~g})}
$$

## Chemicals in liquids or solid states are NOT included in the equilibrium expressions!!

- Liquids and solids have a fixed density and therefore, a fixed concentration.
- The only exception is when two liquids appear in the same equation, thus each liquids dilutes the other.

Balance and write the equilibrium expression for the following reactions:
$\ldots \mathrm{Cr}_{2} \mathrm{O}_{7^{-2}(\mathrm{aq})}{ }^{+} \ldots \mathrm{H}_{2} \mathrm{O}_{(\mathrm{l})} \leftrightharpoons \ldots \mathrm{H}^{+}{ }_{(\mathrm{aq})}+\ldots \mathrm{CrO}_{4}^{2-}{ }_{(\mathrm{aq})} \quad \ldots \mathrm{NaCl}_{(\mathrm{s})} \leftrightharpoons \ldots \mathrm{Na}^{+}{ }_{(\mathrm{aq})}+\ldots \mathrm{Cl}^{-}{ }_{(\mathrm{aq})}$
$\ldots \mathrm{H}_{2(\mathrm{~g})}+\ldots \mathrm{Br}_{2(\mathrm{l})} \leftrightharpoons \ldots \mathrm{HBr}_{(\mathrm{g})}$
$\ldots \mathrm{B}_{2} \mathrm{H}_{6(\mathrm{~g})}+\ldots \mathrm{O}_{2(\mathrm{~g})} \leftrightharpoons \ldots \mathrm{B}_{2} \mathrm{O}_{3(\mathrm{~s})}+\ldots \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})}$

## Hebden Workbook: Pg. 60 \#31, 34, 35:

31. Write the equillbrium expressions for the following.
a) $2 \mathrm{ICl}(\mathrm{g}) \rightleftharpoons \mathrm{I}_{2}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g})$
b) $\mathrm{N}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}(\mathrm{g})$
c) $3 \mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{O}_{3}(\mathrm{~g})$
d) $2 \mathrm{Bi}^{3+}(\mathrm{aq})+3 \mathrm{H}_{2} \mathrm{~S}(\mathrm{~g})=\mathrm{Bi}_{2} \mathrm{~S}_{3}(\mathrm{~s})+6 \mathrm{H}^{+}(\mathrm{aq})$
e) $\mathrm{CaCO}_{3}(\mathrm{~s}) \rightleftharpoons \mathrm{CaO}(\mathrm{s})+\mathrm{CO}_{2}(\mathrm{~g})$
f) $\mathrm{CaC}_{2}(\mathrm{~s})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l})=\mathrm{C}_{2} \mathrm{H}_{2}(\mathrm{~g})+\mathrm{Ca}(\mathrm{OH})_{2}(\mathrm{~s})$
g) $\mathrm{C}_{6} \mathrm{H}_{6}(\mathrm{l})+\mathrm{Br}_{2}(\mathrm{l}) \rightleftharpoons \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Br}(\mathrm{l})+\mathrm{HBr}(\mathrm{g})$
h) $\mathrm{Cu}(\mathrm{s})+2 \mathrm{Ag}^{+}(\mathrm{aq}) \rightleftharpoons \mathrm{Cu}^{2}+(\mathrm{aq})+2 \mathrm{Ag}(\mathrm{s})$
i) $4 \mathrm{NH}_{3}(\mathrm{~g})+5 \mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons 6 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})+4 \mathrm{NO}(\mathrm{g})$
j) $\mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightleftharpoons \mathrm{H}_{2} \mathrm{O}(\mathrm{l})$
32. Which way will the equilibrium $\mathrm{CaCO}_{3}(\mathrm{~s})+\mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftharpoons \mathrm{Ca}^{2+}(\mathrm{aq})+2 \mathrm{HCO}_{3}^{-}(\mathrm{aq})+40 \mathrm{~kJ}$ shift if
(a) more $\mathrm{CO}_{2}(\mathrm{~g})$ is added?
(c) $\mathrm{Ca}^{2+}(\mathrm{aq})$ is removed?
(b) more $\mathrm{CaCO}_{3}$ (s) is added?
(d) heat is added?
33. Rearrange the following equations to solve in terms of the concentrations indicated in bold.
(a) $K_{\text {eq }}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{F}^{-}\right]}{[\mathrm{HF]}}$
(d) $K_{e q}=\frac{\left[\mathrm{NO}_{2}\right]^{2}}{\left[\mathrm{NO}^{2}\left[\mathrm{O}_{2}\right]\right.}$
(g) $K_{\text {eq }}=\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}$
(b) $\mathrm{K}_{\mathrm{eq}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{F}^{-}\right]}{[\mathrm{HF}]}$
(e) $K_{\mathrm{eq}}=\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}$
(h) $K_{\text {eq }}=\frac{\left[\mathrm{PCl}_{3}\right]^{4}}{\left[\mathrm{P}_{4}\right]\left[\mathrm{Cl}_{2}\right]}$
(c) $K_{e q}=\frac{\left[\mathrm{NO}_{2}\right]^{2}}{\left[\mathrm{NO}^{2}\left[\mathrm{O}_{2}\right]\right.}$
(f) $K_{\text {eq }}=\frac{\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]}{\left[\mathrm{NO}_{2}\right]^{2}}$

## Relative Size of Keq $_{\text {eq }}$

Recall that...

$$
\mathrm{K}_{\mathrm{eq}}=\frac{[\text { products }]}{[\text { reactants }]}
$$

| $\mathrm{K}_{\mathrm{eq}}>1$ | $\mathrm{~K}_{\mathrm{eq}}=$ | are favoured. |
| :--- | :--- | :---: |
| $\mathrm{K}_{\mathrm{eq}}<1$ | $\mathrm{~K}_{\mathrm{eq}}=$ | are favoured. |

Which of the following is least likely to favour the formation of products?
A. $2 \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})} \leftrightharpoons 2 \mathrm{H}_{2(\mathrm{~g})}+\mathrm{O}_{2(\mathrm{~g})}$
$\mathrm{K}_{\text {eq }}=7.3 \times 10^{-18}$
B. $\mathrm{N}_{2} \mathrm{O}_{(\mathrm{g})}+\mathrm{NO}_{2(\mathrm{~g})} \leftrightharpoons 3 \mathrm{NO}_{(\mathrm{g})}$
$\mathrm{K}_{\text {eq }}=4.2 \times 10^{-4}$
C. $\mathrm{N}_{2} \mathrm{O}_{4(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NO}_{2(\mathrm{~g})}$
$\mathrm{K}_{\text {eq }}=4.5$
D. $\mathrm{SO}_{2(\mathrm{~g})}+\mathrm{NO}_{2(\mathrm{~g})} \leftrightharpoons \mathrm{NO}_{(\mathrm{g})}+\mathrm{SO}_{3(\mathrm{~g})}$
$\mathrm{K}_{\text {eq }}=85$

Explain your answer to the question above:

## Does the value of $K_{\text {eq }}$ change when...

## Concentration changes?

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})} \quad \Delta \mathrm{H}=-92 \mathrm{~kJ} / \mathrm{mol}
$$

- What happens to the relative concentrations of each species when...
- $\mathrm{NH}_{3}$ is increased?

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})} \quad \mathrm{K}_{\mathrm{eq}}=
$$

Overall, the concentration $\qquad$ stays the same, so $\mathrm{K}_{\text {eq }}$ $\qquad$ .

- $\mathrm{H}_{2}$ is decreased?

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})} \quad \mathrm{K}_{\mathrm{eq}}=
$$

$\qquad$ stays the same, so $\mathrm{K}_{\text {eq }}$ $\qquad$ -.

## Temperature changes?

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})}
$$

$\Delta \mathrm{H}=-92 \mathrm{~kJ} / \mathrm{mol}$

- What happens to the relative concentrations of each species when...
- Heat is increased?

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})}+\text { heat } \quad \mathrm{K}_{\mathrm{eq}}=
$$

Concentration of reactants $\qquad$ .

Concentration of products $\qquad$ .

Therefore, $\mathrm{K}_{\mathrm{eq}}$ will $\qquad$ _.

- Heat is decreased?

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})}+\text { heat } \quad \mathrm{K}_{\text {eq }}=
$$

Concentration of reactants $\qquad$ .

Concentration of products $\qquad$ .

Therefore, $\mathrm{K}_{\mathrm{eq}}$ will $\qquad$ .

## For the following equations, state whether the $K_{\text {eq }}$ would increase or decrease:

| Equation: | Temperature <br> change: | $\mathbf{K}_{\text {eq }}$ result: |
| :--- | :--- | :--- |
| $\mathrm{G}+\mathrm{H} \leftrightharpoons \mathrm{J} \quad \Delta \mathrm{H}=-92 \mathrm{~kJ} / \mathrm{mol}$ | Increase |  |
| $\mathrm{A}+\mathrm{B}+$ heat $\leftrightharpoons \mathrm{C}$ | Increase |  |
| $\mathrm{P}+\mathrm{Q} \leftrightharpoons \mathrm{R}+\mathrm{S}+150 \mathrm{~kJ}$ | Decrease |  |
| $\mathrm{W}+\mathrm{X}+100 \mathrm{~kJ} \leftrightharpoons \mathrm{Y}+\mathrm{Z}$ | Decrease |  |
| $\mathrm{N}+\mathrm{M} \leftrightharpoons \mathrm{P} \quad \Delta \mathrm{H}=+125 \mathrm{~kJ} / \mathrm{mol}$ | Increase |  |

For the following equations, determine whether the reaction is endothermic or exothermic from the observations:

| Equation: | Temperature <br> Change: | $\mathrm{K}_{\mathrm{eq}:}$ | Exo or Endo: |
| :--- | :--- | :--- | :--- |
| $\mathrm{A}+\mathrm{B} \leftrightharpoons \mathrm{C}+\mathrm{D}$ | Increase | Increases |  |
| $\mathrm{E}+\mathrm{F} \leftrightharpoons \mathrm{G}+\mathrm{H}$ | Decrease | Decrease |  |
| $\mathrm{I}+\mathrm{J} \leftrightharpoons \mathrm{K}+\mathrm{L}$ | Increase | Decrease |  |
| $\mathrm{M}+\mathrm{N} \leftrightharpoons \mathrm{O}+\mathrm{P}$ | Decrease | Increase |  |
| $\mathrm{Q}+\mathrm{R} \leftrightharpoons \mathrm{S}+\mathrm{T}$ | Increase | Decrease |  |

For the following equations, determine whether the temperature has increased or decreased:

| Equation: | $\mathbf{K}_{\text {eq }}$ result: | Temperature <br> change: |
| :--- | :--- | :--- |
| $\mathrm{G}+\mathrm{H} \leftrightharpoons \mathrm{J} \quad \Delta \mathrm{H}=-92 \mathrm{~kJ} / \mathrm{mol}$ | Increased |  |
| $\mathrm{A}+\mathrm{B}+$ heat $\leftrightharpoons \mathrm{C}$ | Decreased |  |
| $\mathrm{P}+\mathrm{Q}+150 \mathrm{~kJ} \leftrightharpoons \mathrm{R}+\mathrm{S}$ | Increased |  |
| $\mathrm{W}+\mathrm{X}+100 \mathrm{~kJ} \leftrightharpoons \mathrm{Y}+\mathrm{Z}$ | Decreased |  |
| $\mathrm{N}+\mathrm{M} \leftrightharpoons \mathrm{P} \quad \Delta \mathrm{H}=+125 \mathrm{~kJ} / \mathrm{mol}$ | Increased |  |

## Practice Questions:

1. Balance and write the equilibrium expression for each of the following:
a. $\qquad$ $\mathrm{H}^{+}{ }_{(\mathrm{aq})} \leftrightharpoons$ $\qquad$ $\mathrm{H}_{2(\mathrm{~g})}+\ldots \mathrm{Fe}^{2+}{ }_{(\mathrm{aq})}$
b. $\qquad$ $\mathrm{Cl}_{2(\mathrm{aq})} \leftrightharpoons$ $\qquad$ $\mathrm{I}_{2(\mathrm{~s})}+\ldots \mathrm{Cl}_{(\mathrm{aq})}$
c. $\qquad$ $\mathrm{CaO}_{(\mathrm{s})}+$ $\qquad$ $\mathrm{CO}_{2(\mathrm{~g})} \leftrightharpoons$ $\qquad$ $\mathrm{CaCO}_{3(\mathrm{~s})}$
d. $\qquad$ $\mathrm{CO}_{2(\mathrm{~g})} \leftrightharpoons$ $\qquad$ $\mathrm{CO}_{2 \text { (aq) }}$
e. $\qquad$ $\mathrm{Na}_{2} \mathrm{O}_{(\mathrm{s})} \leftrightharpoons$ $\qquad$ $\mathrm{Na}_{(1)}+$ $\qquad$ $\mathrm{O}_{2(\mathrm{~g})}$
2. A 2.0 L flask contains $0.38 \mathrm{~mol} \mathrm{CH}_{4(\mathrm{~g})}, 0.59 \mathrm{~mol} \mathrm{C}_{2} \mathrm{H}_{2(\mathrm{~g})}$, and $1.4 \mathrm{~mol}_{2(\mathrm{~g})}$ at equilibrium. Calculate the equilibrium constant for the reaction:
$2 \mathrm{CH}_{4(\mathrm{~g})} \leftrightharpoons \mathrm{C}_{2} \mathrm{H}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})}$
3. A cylinder contains $0.12 \mathrm{M} \mathrm{CoBr}_{2}, 0.060 \mathrm{MCO}$, and $0.080 \mathrm{M} \mathrm{Br}_{2}$ at equilibrium. The volume of the cylinder is suddenly doubled.

$$
\mathrm{COBr}_{2(\mathrm{~g})} \leftrightharpoons \mathrm{CO}_{(\mathrm{g})}+\mathrm{Br}_{2(\mathrm{~g})}
$$

a) What is the molar concentration of each gas immediately after the volume of the cylinder is doubled?
b) Explain, in terms of Le Chatelier's principle, why the system shifts right to restore equilibrium.
4. A closed flask contains $0.65 \mathrm{~mol} / \mathrm{L} \mathrm{N}_{2}$ and $0.85 \mathrm{~mol} / \mathrm{L} \mathrm{H}_{2}$ at equilibrium. What is the $\left[\mathrm{NH}_{3}\right]$ ?

$$
\mathrm{N}_{2(\mathrm{~g})}+3 \mathrm{H}_{2(\mathrm{~g})} \leftrightharpoons 2 \mathrm{NH}_{3(\mathrm{~g})} \quad \mathrm{K}_{\mathrm{eq}}=0.017
$$

